

Bayesian methods in health economics

Gianluca Baio

University College London
Department of Statistical Science

`g.baio@ucl.ac.uk`

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- *Health economic evaluation*
 - What is health economics?
 - What does health economics do?

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 - Rationale
 - Main ideas

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 - Main ideas
- *Conclusions*

- **Objective:** Combine **costs** & **benefits** of a given intervention into a rational scheme for allocating resources
 - Recently, models have been built upon more advanced statistical foundations
 - This problem can be formalised within a statistical decision-theoretic approach. Rational decision-making is effected through the comparison of expected utilities
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 - **Incremental** approach: need to consider at least two interventions
- Increasingly under a **Bayesian framework**, especially in the UK: **5.9.10–12 Dealing with parameter uncertainty in cost-effectiveness analysis (NICE Methods for Technology Assessment)**
 - *All inputs used in the analysis will be estimated with a degree of imprecision.*
 - *Probabilistic sensitivity analysis is preferred for translating the imprecision in all input variables into a measure of decision uncertainty in the cost-effectiveness of the options being compared.*
 - *Appropriate ways of presenting uncertainty include confidence ellipses and scatter plots on the cost-effectiveness plane (when the comparison is restricted to two alternatives) and cost-effectiveness acceptability curves.*

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 - Strong positive correlation — effective treatments are innovative and result from intensive and lengthy research \Rightarrow are associated with higher unit costs
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- There are different ways in which we can define (e, c) for a specific problem
 - Direct vs indirect vs intangible costs
 - “Hard-” vs utility-based clinical outcomes
 - Public (e.g. NHS) vs private (e.g. insurance) perspective

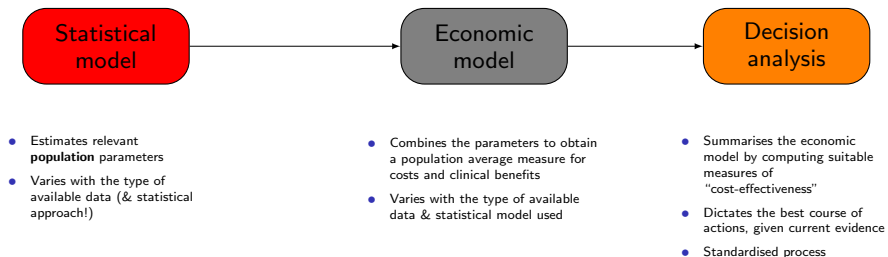
Statistical model

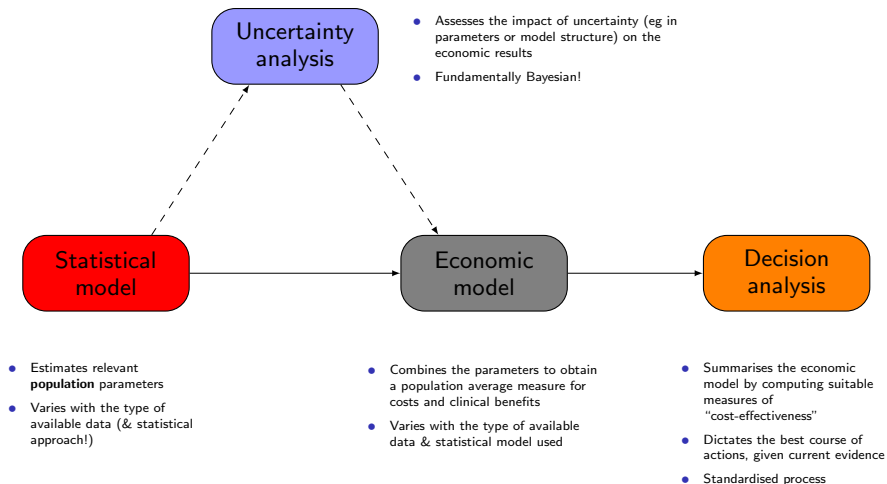
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- Combines the parameters to obtain a population average measure for costs and clinical benefits
- Varies with the type of available data & statistical model used





- **Sampling variability** for the health economic outcomes is described by a distribution $p(e, c | \theta^t)$, which depends on a set of population parameters θ^t
 - Probability of some clinical outcome
 - Duration in treatment
 - Reduction in the rate of occurrence of some event
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- The way in which we construct our statistical model, depends on
 - The characteristic of the available data (**individual-level** vs **aggregated** data)
 - The statistical framework (Bayesian vs frequentist)

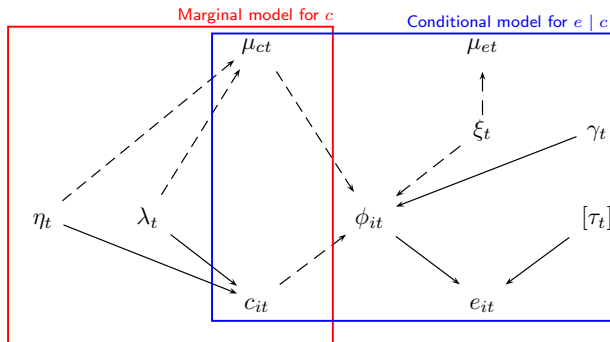
- Observe vectors (e, c) under each intervention being compared
 - May also observe other variables (covariates) — e.g. individual values for age, sex, co-morbidities, etc
- Use observed data to estimate the relevant population parameters
 $\theta^t = (\theta_e^t, \theta_c^t)$
 - These are generally vectors, made by several components (e.g. means, variances, rates, etc)

- The main interest is in the **population average benefits and costs** under treatment t

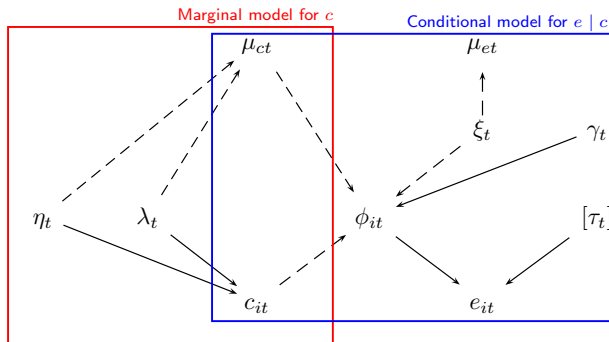
$$\mu_e^t = E[e \mid \theta^t] \quad \text{and} \quad \mu_c^t = E[c \mid \theta^t]$$

- **NB:** Because of underlying correlation, it is necessary to use some form of joint model
 - But: simple models (such as bivariate Normal) are not suitable, as both e, c tend to be skewed and cost are positive

Can factorise the joint distribution, for example as $p(e, c) = p(c)p(e | c)$



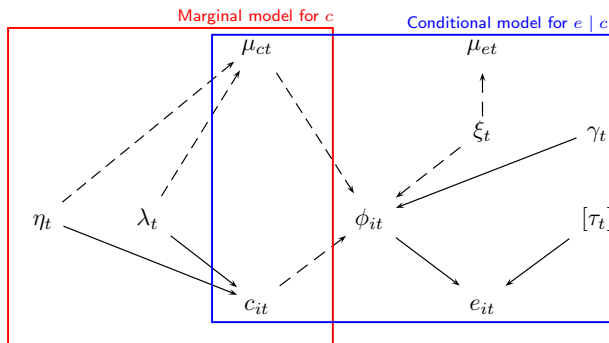
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For instance, can model

- $c_{it} \sim \text{Gamma}(\eta_t, \lambda_t)$ [rate & shape] $\Rightarrow \mu_{ct} = \eta_t / \lambda_t$
- $c_{it} \sim \text{logNormal}(\eta_t, \lambda_t)$ [log mean & log sd] $\Rightarrow \mu_{ct} = \exp(\eta_t + \lambda_t^2 / 2)$

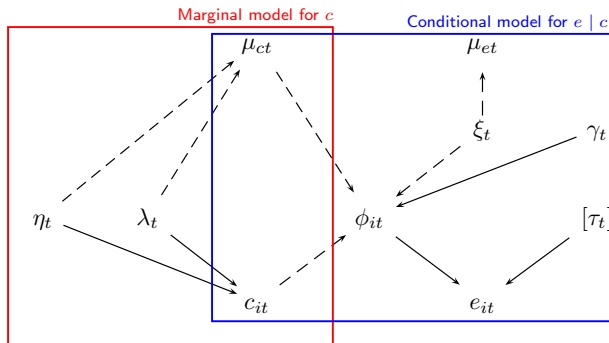
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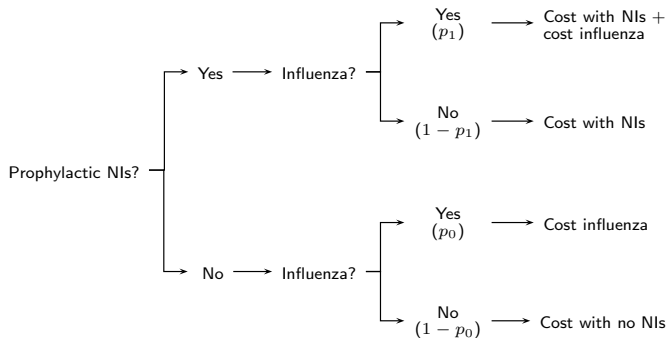
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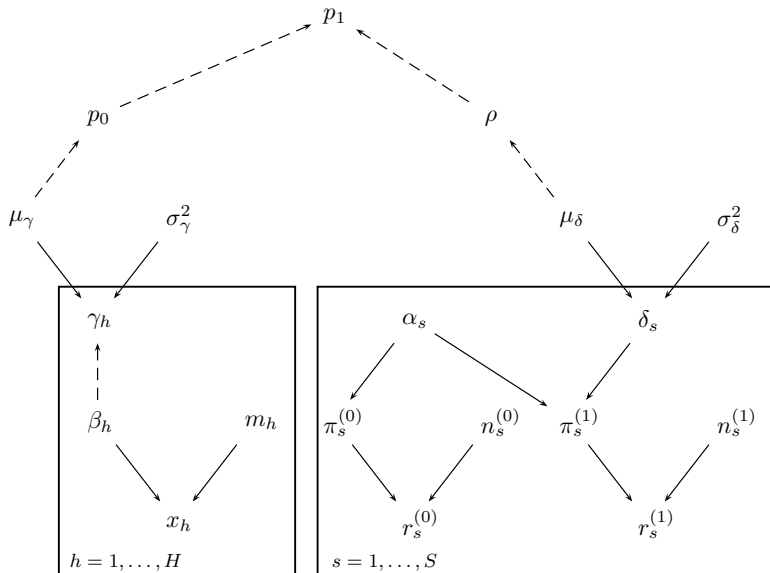
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- $E[e_{it}] = \phi_{it}$; $g(\phi_{it}) = \xi_t + \gamma_t(c_{it} - \mu_{ct}) \Rightarrow \mu_{et} = g^{-1}(\xi_t)$

- Often, we do not have access to individual data and all we have is a set of aggregated data on relevant quantities
- These can in turn be used to construct a “population model” to describe the disease history and its implications
 - Decision trees
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Example: influenza





- Cost minimisation
 - Assumes that the benefits produced by two interventions are identical \Rightarrow the only dimension of interest is costs
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- **Cost-effectiveness analysis (CEA)**
 - Evaluates **cost-per-outcome gained**
 - Outcomes are usually “hard” measurements (eg death) \Rightarrow easy to understand for clinicians, but difficult to compare across diseases (may have different main outcome)
- **Cost-utility analysis (CUA)**
 - Considers a common health outcome unit (= QALYs), so easy to compare across diseases
 - Often interchangeable with CEA (common methodology!)

Can think of this step as the process of obtaining relevant population summaries for the measures of cost & clinical benefits. For example, when comparing two interventions $t = 0, 1$, the main focus is on

- The **increment in mean benefits**

$$\Delta_e = \underbrace{E[e | \theta^1]}_{\mu_1^e} - \underbrace{E[e | \theta^0]}_{\mu_0^e}$$

- The **increment in mean costs**:

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- **NB**: In a Bayesian context, these are functions of θ and thus random variables!
- When using individual-level data, estimation typically directly available from the statistical model; for decision-analytic models, it may be necessary to combine the parameters to obtain these

In order to compare the two interventions ($t = 0, 1$), we define suitable health economic indicators

- The **population average increment in benefits**

$$E[\Delta_e] = \bar{e}_1 - \bar{e}_0 = E[\mu_1^e] - E[\mu_0^e]$$

- The **population average increment in costs:**

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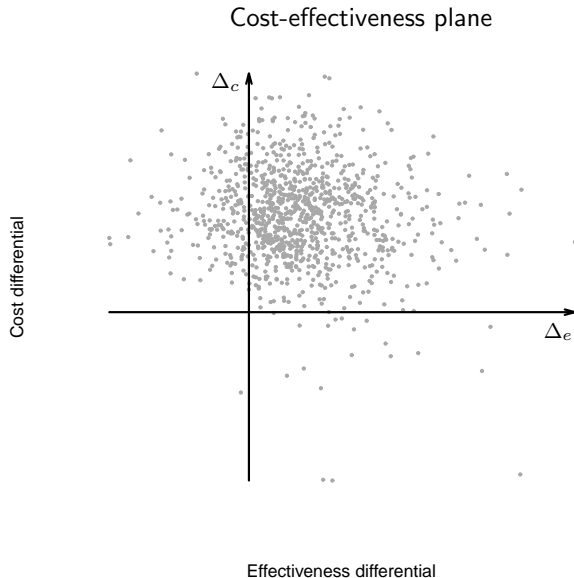
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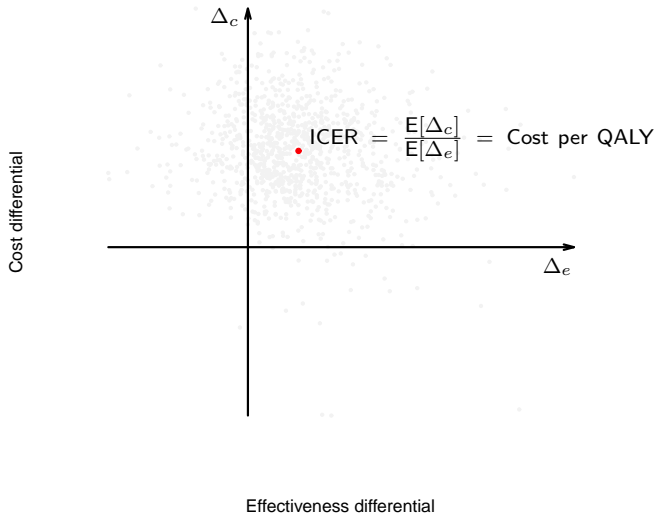
$$E[\Delta_c] = \bar{c}_1 - \bar{c}_0 = E[\mu_1^c] - E[\mu_0^c]$$

- Generally, economic summaries are computed in the form of “cost per outcome” ratios

$$\text{ICER} = \frac{E[\Delta_c]}{E[\Delta_e]} = \text{Additional cost to gain 1 unit of benefit}$$



Cost-effectiveness plane



- When considering only two interventions $t = 0, 1$, can equivalently represent the problem using the *Expected Incremental Benefit*

$$\text{EIB} = k\text{E}[\Delta_e] - \text{E}[\Delta_c]$$

where k is the **willingness to pay**

- Puts costs and benefits on the same scale
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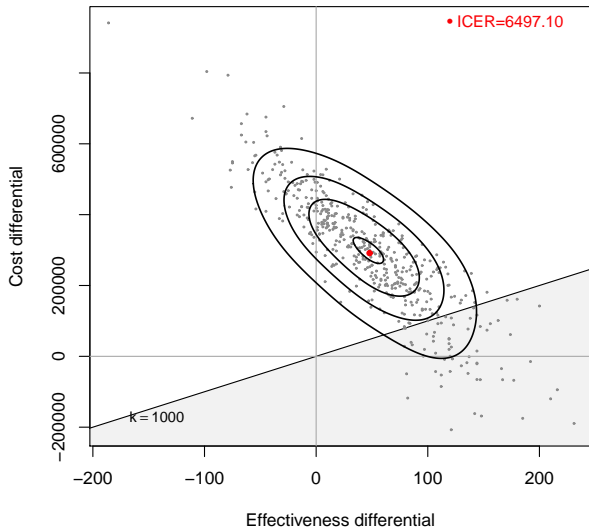
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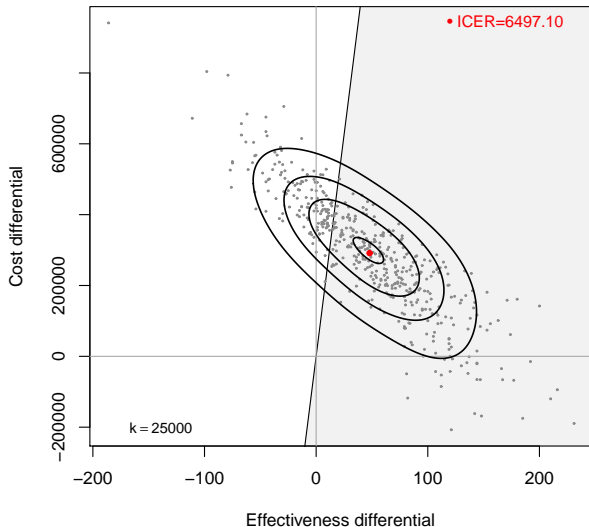
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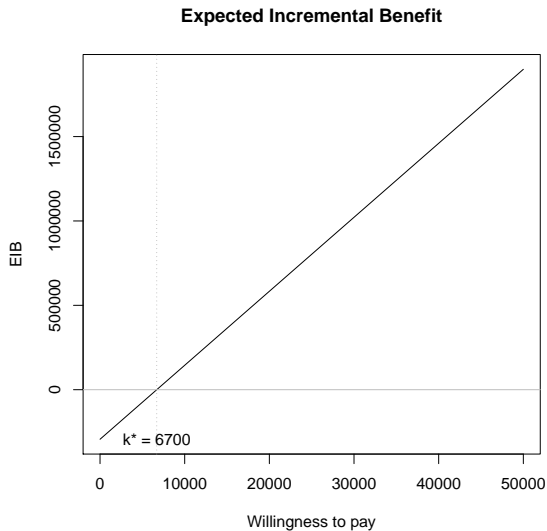
- The EIB is also more directly linked to a (Bayesian) decision-theoretic approach
 - Define a utility function to quantify the “value” of an intervention
 - Compute the expected utility (wrt to both individual & population variations)
 - Choose the intervention with the highest expected utility

Cost effectiveness plane New Chemotherapy vs Old Chemotherapy



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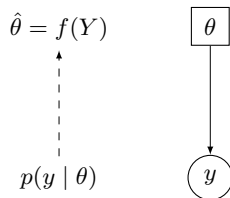
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- The quality of the current evidence is often limited
 - During the pre-market authorisation phase, the regulator should decide whether to grant reimbursement to a new product — and in some countries also set the price — on the basis of uncertain evidence, regarding both clinical and economic outcomes
 - Although it is possible to answer some unresolved questions after market authorisation, relevant decisions such as that on reimbursement (which determines the overall access to the new treatment) have already been taken

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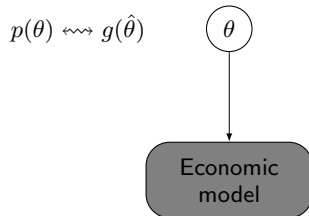
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- This leads to the necessity of performing *(probabilistic) sensitivity analysis (PSA)*
 - Formal quantification of the impact of uncertainty in the parameters on the results of the economic model
 - Standard requirement in many health systems (e.g. for NICE in the UK), but still not universally applied
 - Often limited to *parametric* uncertainty, but should be extended to *structural* uncertainty too

1. Estimation (base-case)



\Rightarrow

2. PSA



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$$\hat{\theta} = f(Y)$$

$$p(y | \theta)$$



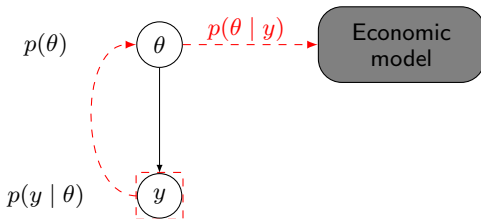
2. PSA

$$p(\theta) \leftrightarrow g(\hat{\theta})$$

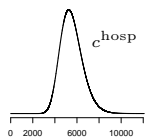
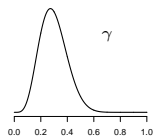
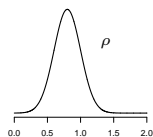
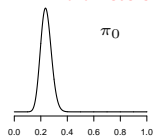


Economic model

Estimation & PSA (one stage)

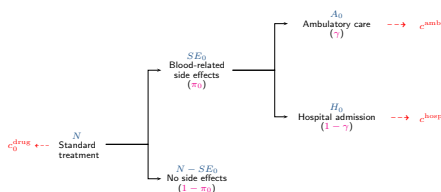


Parameters

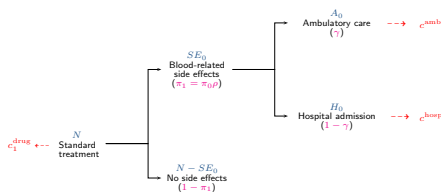


Model structure

$t = 0$: Old chemotherapy



$t = 1$: New chemotherapy

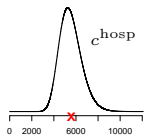
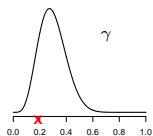
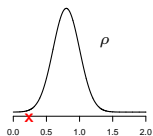
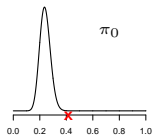


Decision analysis

Old chemotherapy	
Benefits	Costs

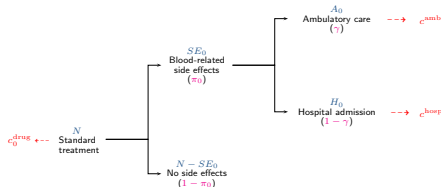
New chemotherapy	
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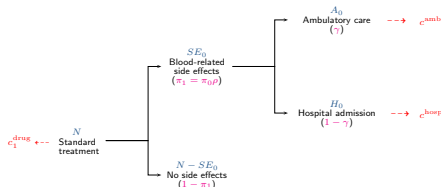
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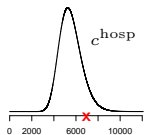
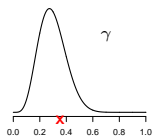
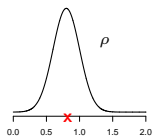
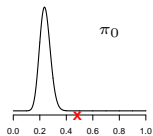
\Rightarrow

Decision analysis

Old chemotherapy	
Benefits	Costs
741	670 382.1

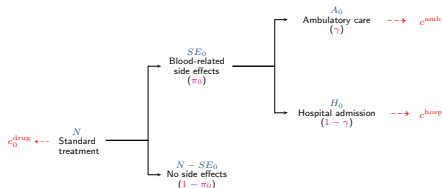
New chemotherapy	
Benefits	Costs
732	1 131 978

Parameters



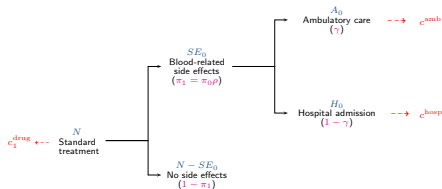
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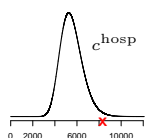
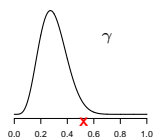
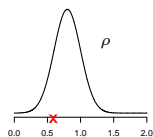
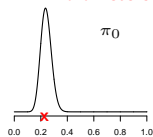
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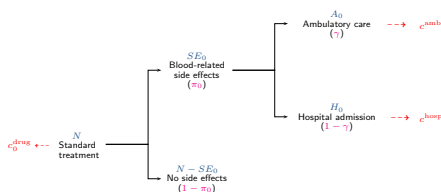
New chemotherapy	
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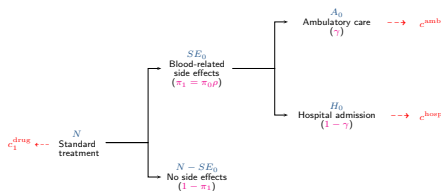
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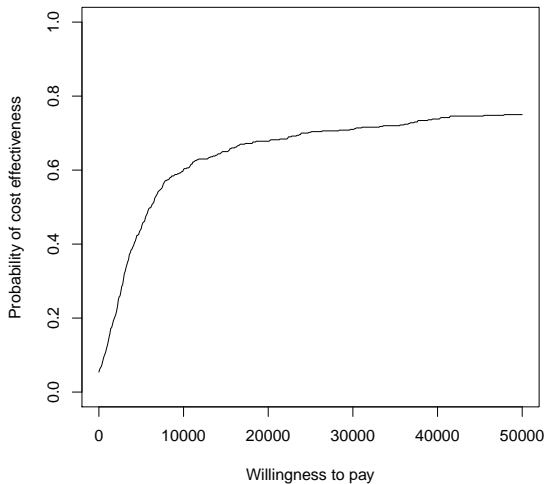
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716.2	790 381.2

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Benefits	Costs
732	1 131 978
664	1 325 654
...	...
811	766 411.4
774.5	1 066 849.8

$$\text{ICER} = \frac{276\,468.6}{58.3} = 6\,497.1$$

Cost Effectiveness Acceptability Curve

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- **Example 2:** Intervention $t = 1$ is the most cost-effective, given current evidence
 - $\Pr(t = 1 \text{ is cost-effective}) = 0.999$
 - If we get it wrong: Increase in costs = £1 000 000 000
Decrease in effectiveness = 999999 QALYs

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- Comments:
 - “Perfect” information is just a hypothetical concept — that is why we consider the “expected value”
 - If the optimal treatment is not dominated at any point in the parameter space, the EVPI is equal to 0 and the uncertainty in the parameters has no impact on the decision process

- Non-intuitive interpretation: when is the EVPI “low enough”?
 - Links with research prioritisation — compare the EVPI with the cost of buying information (e.g. a trial) and decide whether it is worth deferring the decision
 - Depends also on the size of the target population

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 - Links with research prioritisation — compare the EVPI with the cost of buying information (e.g. a trial) and decide whether it is worth deferring the decision
 - Depends also on the size of the target population
- Usually, it is impossible to buy information on **all** the model parameters
 - Some parameters are not even *that* interesting — e.g. fixed costs, “things” we cannot change, ...
 - Some other though, are interesting, because we can conduct a study to learn more and thus potentially change the optimal decision
 - Can consider the **Expected Value of Partial Perfect Information**

- Suppose the parameters of your model are collected in a vector θ
- And that you can split them into two subsets
 - The “important” parameters ϕ and the “unimportant” parameters ψ
- We are interested in quantifying the value of gaining more information on ϕ , while leaving the current level of uncertainty on ψ unchanged

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- **Technical issue:** because ϕ and ψ are typically correlated, we cannot make easy computations for the EVPPI (certainly not in Excel!)
 - Nested Monte Carlo simulations
 - ① Simulate a large number of values for ϕ
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 - ③ This means we may need to run a PSA with $10\,000s \times 10\,000s$ iterations — too big!
 - New methods based on “non-parametric regression” (fancy stats)
 - Can use a standard run of 1 000 PSA simulations and can approximate the true value of the EVPPI very accurately!

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 - Useful in the case of individual-level data (eg from Phase III RCT)
- Using MCMC methods, it is possible to produce the results in terms of simulations from the posterior distributions
 - These can be used to build suitable variables of cost and benefit
 - Particularly effective for running “probabilistic sensitivity analysis”

Thank you!



Baio, G. (2012),
Bayesian Methods in Health Economics.
Chapman Hall, CRC Press, Boca Raton, FL.



Briggs, A., M. Sculpher, and K. Claxton (2006).
Decision modelling for health economic evaluation.
Oxford University Press, Oxford, UK.



Heath, A., I. Manolopoulou, and G. Baio (2015).
Efficient High-Dimensional Gaussian Process Regression to calculate the Expected Value of Partial Perfect Information in Health Economic Evaluations.
<http://arxiv.org/abs/1504.05436v1>.



Jackson, C., L. Sharples, and S. Thompson (2010).
Structural and parameter uncertainty in Bayesian cost-effectiveness analysis.
Journal of the Royal Statistical Society, C 59, 233–253.



Spiegelhalter, D., K. Abrams, and J. Myles (2004).
Bayesian Approaches to Clinical Trials and Health-Care Evaluation.
John Wiley and Sons, Chichester, UK.



Strong, M., J. Oakley, and A. Brennan (2014).
Estimating Multiparameter Partial Expected Value of Perfect Information from a Probabilistic Sensitivity Analysis Sample A Nonparametric Regression Approach.
Medical Decision Making 34(3), 311–326.



Welton, N., A. Sutton, N. Cooper, K. Abrams, and A. Ades (2012).
Evidence Synthesis for Decision Making in Healthcare
John Wiley and Sons, Chichester, UK.