

## ISPOR Europe 2019 – Short course

### [Probabilistic graphical models with OpenMarkov, an open-source tool](#)

**Presenter:** [Francisco Javier Díez](#), PhD  
Dept. Artificial Intelligence, UNED, Spain  
[fjdiez@dia.uned.es](mailto:fjdiez@dia.uned.es).

Hands-on exercises to be done with [OpenMarkov](#) during the course. You must download the file [exercises.zip](#) and uncompress it where you can easily find the files it contains. We strongly recommend you not to look at the solutions before you try to solve the exercises.

We also recommend you to read through the **hints** we offer for each exercise before you start reproducing them in OpenMarkov.

## 1. Probabilistic diagnosis

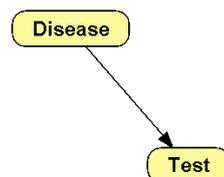
### Exercise

The prevalence of a disease in a certain subpopulation is 14%. There is a test for this disease with a sensitivity of 70% and a specificity of 91%.

- What is the positive predictive value of the test?
- What is the negative predictive value?

### Hints

- We will create a Bayesian network with two nodes, *Disease* and *Test*, and introduce evidence on the second in order to compute the posterior probabilities of the disease given the test result.
- Create a new network with button . Check that **Network type** is *Bayesian network*.
- Create a chance node by clicking on button  and then clicking where you wish to place it. Double-click on this node to open the **Node properties** dialog and change its name to *Disease*. In the **Domain** tab, check that the **states** are *present* and *absent*. Click OK.
- Create the node *Test* similarly. In the **Domain** tab, assign the states *positive* and *negative*, either by writing the names in the corresponding cells or by selecting them with the **Standard domains** button.
- Select the button  and draw a link by dragging the pointer from node *Disease* to node *Test*, as shown in the next figure.



- If you wish to move a node, select it with button  and drag it.
- Edit the probability table for *Disease*, either by alt-clicking on this node or by right-clicking on it and selecting the **Edit probability** option. In the upper cell, write *0.14*, the prevalence given in the statement of the problem, which is the probability of the disease being present.

- Edit the probability table for *Test*. In the upper right cell, write the sensitivity, 0.70, which is the probability of a positive result when the disease is present. In the lower left cell write the specificity, 0.91, which is the probability of a negative result when the disease is absent.
- Save the network as *BN-one-test.pgm*x, checking that the file type is *ProbModel 0.2 (\*.pgm)*x.
- Compile the network with the  button.
- Introduce the finding *Test = positive* by double-clicking on the state *positive* of node *Test*. The positive predictive value is the probability of *Disease = present*. This will answer the first question in the statement of the problem.
- Introduce the finding *Test = negative*. The negative predictive value is the probability of *Disease = absent*. This will answer the second question.

## 2. Learning Bayesian networks

### Exercise

- Learn different Bayesian networks from the dataset *asia10K.csv*, contained in file [exercises.zip](#), using two algorithms: *hill-climbing* and *PC*.
- This dataset contains 10,000 fictitious patients. They were randomly generated by probabilistic sampling from the network *BN-asia.pgm*x, also included in [exercises.zip](#). We will learn a Bayesian network as if we didn't know the true model that generated the data.

### Hints

- We recommend that you first open the network *BN-asia.pgm*x (the “true” model) with OpenMarkov and then the dataset *asia10K.csv* with a text editor, to gain some insight about it. The first line of the dataset contains the names of the variables and each of the following lines contains the values for a case (a patient).

#### *Learn a Bayesian network with the hill-climbing algorithm*

- In OpenMarkov, go to **Tools > Learning** and select the dataset *asia10K.csv*. Check that, by default, the algorithm is *hill-climbing* and the metric is *K2*. The alpha parameter (Laplace-like correction) will be used when estimating the parameters of the network, not when learning the structure.
- Click **Learn**. By default, OpenMarkov will place the nodes in a circle.
- You can accept the edits proposed by OpenMarkov or choose your own, either by selecting one from the list or by drawing/removing links from the graph. Please note that every time the network is modified, the list of edits is updated.
- Save the network learned if you wish.

#### *Learn a Bayesian network with the PC algorithm*

- Go again to **Tools > Learning** and replace **Hill climbing** with **PC**. Check that initially the significance level is 0.05.
- Click **Learn**. Accept one by one all the edits proposed by OpenMarkov. Observe that the algorithm has three phases: removing links, orienting pairs of links that converge on a node, and orienting the rest of the links.
- Apply again the PC algorithm for different values of the significance level—for example, 0, 0.001, 0.01, 0.1, 0.5, 0.7, 0.9, 0.99, and 1. You can set it by clicking the **Options** button after selecting the PC algorithm. Count the number of links in the resulting network for each significance level.

### 3. Unicriterion decision analysis

#### Exercise

- For a certain disease, whose prevalence is 2%, there are two tests, with the following properties:

Test	sensitivity	specificity	discomfort	cost
A	0.60	0.92	0.0003 QALY	\$100
B	0.80	0.91	0.0001 QALY	\$200

- There is also a therapy, costing \$7,000. The effectiveness is:

Disease →	absent	present
therapy	38 QALY	30 QALY
no therapy	40 QALY	20 QALY

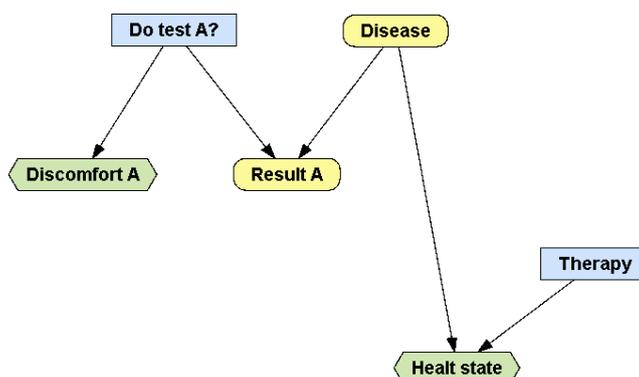
- What is the most effective strategy?

#### Hints

- Given that the goal is to maximize the effectiveness, we disregard costs at the moment. (We will consider them in the next exercise, which is a cost-effectiveness analysis for the same problem.)

Create the structure of the network (including only test A)

- Click the button  to create a new model. Network type must be *Decision analysis network*.
- Right-click anywhere on the empty panel to open the Network properties dialog. Go to tab *Advanced*, select *Decision criteria*, *Standard criteria*, and *Cost-effectiveness (\$/QALY)*.
- Create the chance node *Disease*; its domain will have the default values, *present* and *absent*.
- Create the chance node *Result A*, with domain  $\{positive, negative\}$ . You may use the *Standard domains* button.
- Create the decision node *Do test A?*. Check that its domain is  $\{yes, no\}$ , the default for decision nodes.
- Create the utility node *Discomfort A*. In the Network properties dialog, the Decision criterion must be "*Effectiveness (QALY)*".
- Create the decision *Therapy*.
- Create the utility node *Health state*, whose Decision criterion is also *effectiveness*.
- Draw the causal links, as in the next. Remember that you can use the button  to select and move nodes, and the button  to draw links.



- Save the network so that you don't lose your work by accident. The name can be, for example, *DAN-two-tests.pgm*.
- Right-click on the link *Do test A? → Result A* and select **Add restrictions**. Mark the two cells in the left column of the table to indicate that when the test is not done, the result is neither *positive* nor *negative*. The table will look as follows:

Link Restriction: Link between Do test A? and Result A		
Do test A?	no	yes
positive	0	1
negative	0	1

- Right-click again on the link *Do test A? → Result A*, select **Edit revelation conditions**, and mark the checkbox for *yes* to indicate that when the test is done, the result (either positive or negative) is known.

#### Introduce the numerical parameters

- Open the probability table for *Disease*. Remember that you can do it by alt-clicking or right-clicking on the node. Introduce the prevalence, 0.02.
- Open the probability table for *Result A*. Introduce the sensitivity and specificity of the test, as shown below. You might need to reorder the parents with the **Reorder variables** button so that the row for *Do test A* appears above the row for *Disease*.

Node Potential: Result A				
		Relation Type: Table		Reorder variables
Do test A?	no	no	yes	yes
Disease	absent	present	absent	present
positive	0	0	0.08	0.6
negative	0	0	0.92	0.4

- Open the utility table for *Health state*. Set **Relation type** to *Exact* and introduce the numeric values, as follows:

Node Potential: Health state				
		Relation Type: Exact		Reorder variables
Therapy	no	no	yes	yes
Disease	absent	present	absent	present
Health state	40	20	38	30

- Open the utility table for *Discomfort A*. Set **Relation type** to *Exact* and introduce the numeric values: when the test is done, the discomfort is  $-0.0003$  QALY (a negative effectiveness); when the test is not done, there is no discomfort.
- Save the network again.

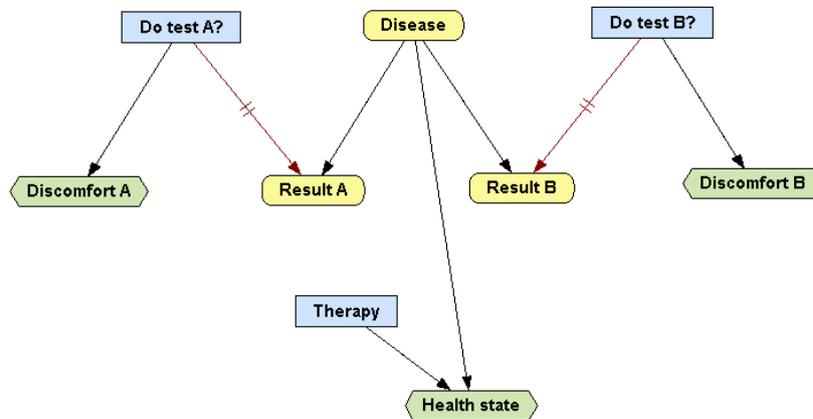
#### Evaluate the model

- Click the button  to expand the decision tree. Observe that the option **Unicriterion** is selected. It means that OpenMarkov will convert cost and effectiveness into a single criterion. In this example there is no cost, so the only criterion will be the effectiveness. Therefore, you must select *QALY* as the unit. Click **OK**.
- The optimal strategy can be obtained by inspecting the tree and selecting for each decision node the branch that maximizes the effectiveness, which is marked with a red rectangle.

- Another way to get the optimal policy (i.e., an alternative to expanding the decision tree and inspecting it) is to click the **S** button: OpenMarkov will show the optimal strategy as an intervention tree, which is much more compact than the decision tree.

Add test B and evaluate the model again

- Add now the three nodes (chance, decision, and utility) for test B and the corresponding links, as you did for test A. The network should look like this:



- Save the network as *DAN-two-tests-without-costs.pgm*.
- If you do not have enough time, open the network *DAN-two-tests-without-costs.pgm*, available in [exercises.zip](#), in the folder *solutions*.
- Find the optimal strategy for this case.

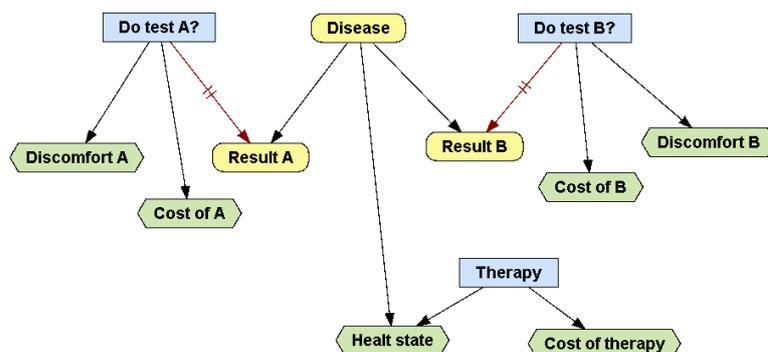
## 4. Cost-effectiveness analysis (atemporal)

### Exercise

- Given the disease and the tests described in the previous exercise, what is the optimal strategy for each value of the willingness to pay?

### Hints

- Depart from the network *DAN-two-tests-without-costs.pgm* built in the previous exercise.
- Add the nodes *Cost A*, *Cost B*, and *Cost therapy*, as shown below. Check that the criterion is *Cost* (\$) for each of them. Draw the links required and edit the corresponding utility tables. (Note that, even though discomfort was introduced as a negative effectiveness, all costs are positive.)



- Save the network as *DAN-two-tests-with-costs.pgm*.
- Click the button  to do a cost-effectiveness analysis. Answer the above question.

### Additional questions

- Would it be possible to solve this problem with an influence diagram? Why?
- Try to build a decision tree *with* embedded decision nodes for this problem. How many leaves would it have?
- Try to build a decision tree *without* embedded decision nodes. How many strategies are there? How many leaves would the tree have?
- If there were *two therapies* instead of one, how many leaves would the tree with embedded decision nodes have? How many strategies would there be? How many leaves would the tree without embedded decision nodes have?

## 5. Cost-effectiveness analysis with a Markov model

### Exercise

- A disease D may be latent or active. When it is latent, the probability of becoming active in the next month is 11% and that of dying is 2%. When the disease is active, the monthly probability of dying is 15%. Quality of life is 0.9 for latent and 0.7 for active disease. The cost of the standard therapy is £150/month when the disease is latent and £2,500/month when it is active.
- There is a new therapy, with a cost of £950/month, which slows down the progression of the disease, so that the monthly probability of becoming active reduces to 8%, without affecting the probability of death. Unfortunately, this therapy has no effect when the disease is already active.
- With an annual discount rate of 3.5% for both cost and effectiveness, what is the ICER of the new therapy?
- Is it cost-effective for a willingness-to-pay of £20,000 per QALY?

### Hints

Check that the model offered in the solutions is correct

- Open the network *MID-latent-active.pgm*, available in [exercises.zip](#), in the folder *solutions*.
- Right-click on an empty zone of the network panel to open the Network properties dialog. Check that Network type is *Markov influence diagram (MID)*.
- In the same Network properties dialog, go to tab *Advanced*, click the button *Decision criteria*, and check that *cost* is measured in *British pounds* and *effectiveness* in *QALYs*. Go back to the *Advanced* tab, click *Temporal options* and check that the cycle length is *1month*.
- Open the Node properties dialog for the chance node *State [0]*. Observe that name is *State* and time slice is *0*. In the *Domain* tab, observe that the states are *latent*, *active*, and *dead*.
- Open the Node properties dialog for the decision node *Therapy* and check that time slice is *atemporal* because this decision is made once and forever. In the *Domain* tab of the same dialog check that the options (the states) for this decision are *new* and *standard*.
- Open the Node properties dialog for *Cost of therapy [0]* and check that its criterion is *Cost (£)*.
- Similarly, check that the criterion for *Quality of life [0]* is *Effectiveness (QALY)*.
- Check that the links are correct. For example, the links pointing at *State [1]* mean that the patient's state in one cycle depends on the state in the previous cycle and (if the patient was in latent state) on whether the therapy is applied. There is no link from *Therapy* to *Quality of life [0]* because the therapy has no direct effect on quality of life: it acts indirectly by delaying the transition from latent to active.

- Open the probability table for *State [0]*. Check that initially all patients are in state *latent* because this is the subpopulation of interest (when the disease is active or the patient is dead, it is not necessary to do a cost-effectiveness analysis to decide that the therapy should not be applied).
- Open the probability table for *State [1]* and check that the transition probabilities agree with the statement of the problem.
- Open the utility table for *Cost of therapy [0]* and check that it is correct. Do the same for *Quality of life [0]*.

#### Temporal evolution of the variables

- Right-click on *State[0]* or *State [1]* and select Temporal evolution. Set the horizon to *60 cycles*, i.e., 5 years, and accept the default value, **One decision**. You will obtain 6 curves showing the probability of each state along time depending on the therapy applied.

If you wish to know the probability of being alive in a cycle (i.e., the proportion of patients that are alive), uncheck the box for *dead* and click the radio button **Sum**; this way OpenMarkov will show the sum of the probabilities of *latent* and *active*. The new therapy clearly increases life expectancy. If you wish to know the probability of the disease being *active* in each cycle, also uncheck the box for *latent*. You will see that the new therapy make patients transition more slowly to state *active*.

- Observe the temporal evolution of *Cost of therapy*. This cost decreases as patients transition from *latent* (the only state in which the new therapy is applied) to the states *active* or *dead*. Click the **Cumulative** radio button to obtain the accrued cost and observe that, as expected, it is higher for the new therapy.
- Observe the temporal evolution of *Quality of life*. Click the **Cumulative** radio button and check that the new therapy increases the effectiveness.

#### Cost-effectiveness analysis

- Click the button . Each discount can be set per year or per cycle. In accordance with the statement of the problem, both discounts are set to *3.5% per year*. OpenMarkov will transform them into per-cycle discounts.

In the **Scope selector**, accept the default value, *One decision*. The **Analysis** tab shows the cost and effectiveness of each intervention. The **CE plane** tab shows them on a plot. On the upper right corner you can set the **Display** relative to *standard* therapy in order to observe the incremental cost and effectiveness of the new therapy. The **Frontier interventions** tab shows these values in a table, as well as the ICER we were looking for, which is £4,678.30 per QALY.

## 6. Sensitivity analysis

### Exercise

- The effect of the new drug analyzed in the previous exercise was obtained from a randomized control trial involving 800 volunteers in latent state. Half of them received the standard therapy for one month; 8 died and 44 transitioned to active disease. The other half received the new therapy for one month; 8 died (as many as in the other group) but only 32 transitioned to active disease.
- The uncertainty about the cost of the new therapy is modeled by a Gamma distribution with a mean of £950 and a variance of 20% of the mean.
- Draw the acceptability curve. Is the new therapy cost-effective for a willingness-to-pay of £20,000/QALY?
- What is the probability of the new therapy being more effective than the standard one?

## Hints

Check that the model offered in the solutions is correct

- Open the network *MID-latent-active-uncert.pgm*, available in [exercises.zip](#), in the folder *solutions*. This file only differs from *MID-latent-active.pgm* in that it has parametric uncertainty.
- Open the probability table for *State [1]*. The red triangles denote the cells whose values are uncertain. Right-click on any cell in the *latent-standard* column and select *Edit uncertainty*. OpenMarkov will show a Dirichlet distribution whose parameters correspond to the 400 patients in latent state who received the standard therapy. Do the same check for the *latent-new* column.
- Open the utility table for *Cost of therapy [0]*. Right-click on the *latent-new* cell. Observe that the uncertainty about the price is model by the Gamma distribution mentioned in the problem statement.

Perform a probabilistic sensitivity analysis

- Click the button . Check that the type of analysis is *Cost-effectiveness*. (If the type of analysis were *Unicriterion*, OpenMarkov would offer other sensitivity analysis options, such as tornado diagrams, plots, etc.) Click OK.
- In the next dialog, observe that OpenMarkov will run 1,000 simulations. Click OK and wait.
- OpenMarkov will show a scatter plot on the cost-effectiveness plane. On the upper right corner you can set the **Display** relative to *standard* therapy. This way the plot will show the incremental cost and effectiveness of the new therapy (in blue) with respect to the standard one (in red) for each simulation.
- Select the tab **Acceptability curve**. Observe that for a willingness to pay (WTP) of £20,000/QALY the probability of the new therapy being cost-effective is around 82%. You can see it more clearly if at the upper left corner you set the **WTP of reference** to that threshold.
- Setting the **WTP of reference** to a very high value (for example, £10,000,000/QALY) is equivalent to aiming at the most effective therapy, regardless of its cost. In this case the probability of the new therapy being cost-effective is just the same as the probability of being effective. OpenMarkov shows that it is around 88%. This corresponds to the proportion of simulations that lie at the right of coordinate axis in the scatter plot we obtained when setting the **Display** relative to *standard* therapy.